Closing Tues: HW 14.2 (part 2)
Closing Thur: HW 14.3/4 (last HW)
Final: Sat, March 10, 5:00-7:50pm,
Final Room is based on quiz section
For BC/BD, AC/AD: PAA A102
For $A A / A B, B B$ PAA A118
For BA: PAA A110

Entry Task:
Find all critical points of

$$
z=f(x, y)=2 x^{4}+y^{2}-4 x y+1
$$

You do (HW Problem 14.2/5)
$z=-6 x^{2}+2 x-4 y^{2}-3 y+8 x y+30$
a. Find the critical point.
b. Find the largest and smallest values of $f(2, y)$ on the interval $y=-4$ to $y=0$.
c. Suppose $(x, y)=(-6,-7)$.

A small increase in $x$ will lead to a LARGER/SMALLER increase in $z$ than a small increase in y . (circle either larger or smaller)
d. Which is steepest at $x=1$ ? $f(x, 4), f(x, 6), f(x, 8)$ or $f(x, 10)$

## Example (From HW 14.2/6)

Find the critical point for

$$
f(x, y)=12+x y+\frac{27}{x}+\frac{8}{y}
$$

## More Applications

Cost Breakdown (14.3/1-2)
Suppose the cost to produce ONE item is given by:

$$
C(x, y)=3 x^{2}+4 y^{2}+5 x y+10
$$

where
$x=$ cost for 1 hour of labor, and
$y=$ cost for 1 pound of materials.

Question:
The current hourly rate for labor is \$20 and material is $\$ 55$ per pound. How will a $\$ 1$ per hour raise for labor affect the cost to produce 1 item?

Marginal Productivity (14.3/5-6)
Suppose that the number of crates of a particular fruit produced is

$$
z=\frac{9 x y-0.0002 x^{2}-5 y}{0.03 x+4 y}
$$

where
$x=$ number of hours of labor, and
$y=$ number of acres of the crop.
Find the marginal productivity of the number of hours of labor when
$x=100$ and $\mathrm{y}=200$.
Interpret your answer

## Combined (Joint) Revenue and Cost

Next time....

